

# COINCIDENCE MIXER FOR FREQUENCY SYNTHESIZER

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**Abstract:** Frequency synthesizers are an essential part of any modern transceiver system. They generate clock and oscillator signals needed for up and down conversion. The fine frequency resolution, low spurious signals, accuracy and stability are most important for these devices. In this paper, the new frequency synthesizer architecture based on direct synthesis and coincidence mixer is presented. The simulation results are also shown.

**Key words:** Frequency synthesizer, Mixer, Oscillator, Phase locked loop,

## INTRODUCTION

Several different frequency synthesis techniques have been presented in the literature over the years. They can be quite clearly divided into three separate categories, namely direct analog synthesis, direct digital synthesis, and indirect analog synthesis. In this context, “indirect” refers to a system based on some kind of a feedback action, whereas “direct” refers to a system having no feedback. One of the most frequently used indirect synthesizer types is the phase-locked loop (PLL). Phases of two signals, i.e. from an external reference and a feedback signal from an oscillator are compared in a phase and frequency detector. Any phase difference will be converted into a voltage by means of a charge pump. A succeeding loop filter extracts the DC component of this voltage, which is then used to control the output signal frequency of a voltage-controlled oscillator (VCO). A PLL provides high output frequency accuracy at reasonable short settling times [1], [2], [3].

In direct analog synthesizer the frequency resolution is achieved by mixing signals of certain frequencies, and then dividing the resulting frequency down. Theoretically, this process can be repeated arbitrarily many times to achieve a finer frequency resolution. Advantages of the direct analog synthesis are very fast switching times and, in theory, arbitrarily fine frequency resolution. However, this technique requires a very large amount of hardware. Also noise is a problem in direct analog synthesis [4]. An alternative architecture for frequency generation is the direct digital synthesis (DDS), e.g. [5], [6]. The output signal is generated in the digital domain with the help of accumulators and a ROM before it is converted to an analog output signal in a D/A

converter. The advantages of direct digital synthesizers are good frequency resolution and very fast settling time while showing low spurious noise. As most of the DDS architecture is digital, a high degree of integration can be achieved. However, the accumulator clock must be faster (at least two times) than the generated output frequency which limits the use of DDS applications [7], [8].

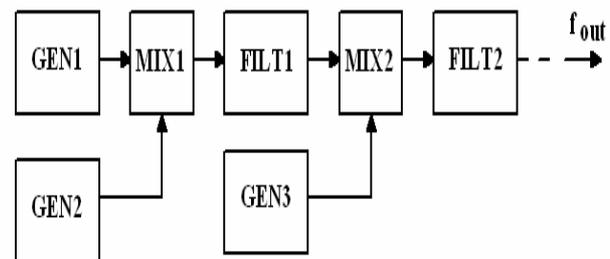


Fig. 1. The block diagram of a conventional direct analog frequency synthesizer. GEN - generator, MIX - mixer, FILT - bandpass filter.

## 1 FINE STEP DIRECT SYNTHESIZER

The block diagram of a conventional direct analog frequency synthesizer is shown in Fig. 1. In this paper frequency synthesizer is based on programmable dividers, multipliers (based on PLL) and coincidence mixers, therefore no filters are need for this synthesizer. For this architecture, Cantor series approximations and Diophantine equations theory are used fine frequency step generation [9].

Let  $N_1, N_2, \dots, N_k$  be relatively prime positive integers (GCD - Greatest common divisor of  $N_1, N_2, \dots, N_k=1$ ). Then for every integer  $u$ , there exist a  $k$  integers  $X_1, X_2, \dots, X_k$ , solving the linear Diophantine equation:

$$\frac{X_1}{N_1} + \frac{X_2}{N_2} + \dots + \frac{X_k}{N_k} = \frac{u}{N_1 N_2 \dots N_k} \quad (1)$$

If  $N_1, N_2, \dots, N_k$  are relatively prime positive integers, then for every integer  $u$  such that:

$$-N_1 N_2 \dots N_k \leq u \leq N_1 N_2 \dots N_k \quad (2)$$

the equation (1) has a solution  $(X_1, X_2, \dots, X_k)$ , where:  $-N_i \leq X_i \leq N_i$  for all  $i=1,2,\dots,k$ .

It is important to say, that equation (1) has a  $k$  solutions (for  $-N_i \leq X_i \leq N_i$ ).

*Example 1:*

Let  $N_1=7, N_2=9, N_3=11$  and  $u=1$ . The solutions of (1) are shown in Tab. 1.:

$X_1$	$X_2$	$X_3$	Sum
-6	2	7	89
1	-7	7	99
<b>1</b>	<b>2</b>	<b>-4</b>	<b>21</b>

Tab. 1. Example of solution (1) for  $N_1=7, N_2=9, N_3=11$  and  $u=1$ . Solution  $[1, 2, -4]$  is optimal.

In Tab. 1., numbers in column "Sum" are computed according (3):

$$Sum = \sum_{i=1}^k X_i^2 \quad (3)$$

and optimal value is minimal according eq. (3). Therefore, *Example 1* has 3 solutions:

$$(1/7)+(2/9)+(-4/11) = (-6/7)+(2/9)+(7/11) =$$

$$(1/7)-(7/9)+(7/11) = 1/(7*9*11) = 1.443 \cdot 10^{-3}$$

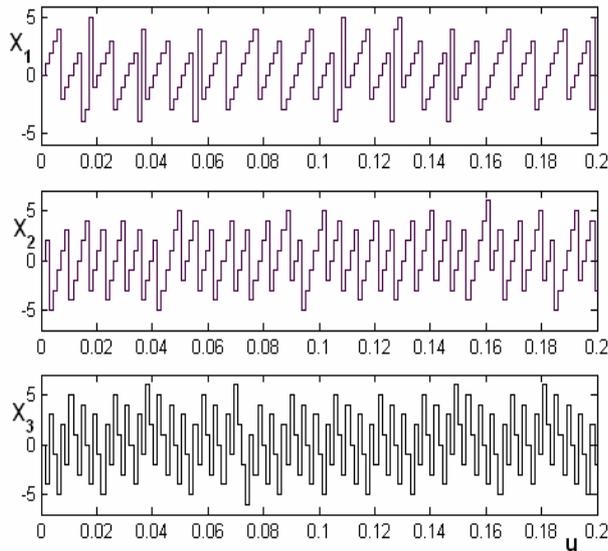


Fig. 2. Optimal values of  $X_1, X_2, X_3$  for Example 1 and  $u/(N_1 N_2 N_3) = \langle 0, 0.2 \rangle$ .

*Example 2:*

Let  $N_1=7, N_2=9, N_3=11$  and  $u=10$ . The optimal solution of (1) is:  $[-4, 2, 4]$  (also  $[3, -7, 4]$  and  $[3, 2, -7]$ ).

Optimal values of  $X_1, X_2, X_3$  for values  $N_1=7, N_2=9, N_3=11$  and  $u/(N_1 N_2 N_3) = \langle 0, 0.2 \rangle$  are shown in Fig. 2.

For frequency synthesizer consist of  $k$  dividers and multipliers the minimal frequency and minimal frequency step is given by (4):

$$Frequency\_step = \frac{f_{REF}}{\prod_{i=1}^k N_i} \quad (4)$$

For *Example 1*,  $Frequency\_step = 1.443 \cdot 10^{-3} f_{REF}$ , and the hardware implementation part of  $(X_i/N_i)$  is shown in Fig. 3. This circuit can be simplified according Fig. 4.

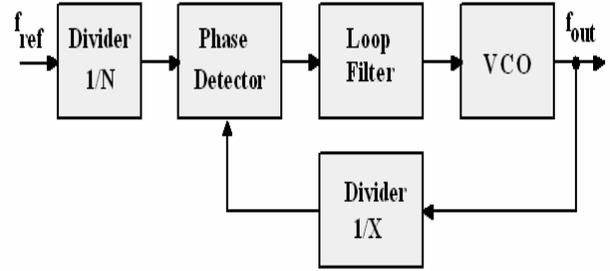


Fig. 3. Simplified hardware implementation of  $(X/N)$  part.

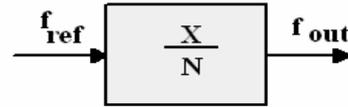


Fig. 4. The  $(X/N)$  part of Fig. 3 as a single block.

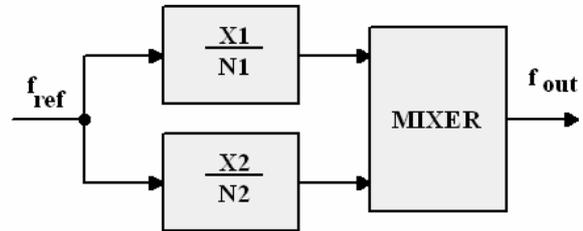


Fig. 5. The block diagram of synthesizer part (with mixer).

Output frequency  $(X/N)$  part (Fig. 3) is given by (5):

$$f_{OUT} = \frac{X_i}{N_i} f_{REF} \quad (5)$$

Synthesizer part block diagram is shown in Fig. 5. Output frequency (Fig. 5) if given by (6):

$$f_{OUT} = \left( \frac{X_1}{N_1} + \frac{X_2}{N_2} \right) f_{REF} \quad (6)$$

The block diagram of final version of frequency synthesizer with 3 " $(X/N)$ " blocks is shown in Fig. 6. Output frequency of this synthesizer (for 3 blocks of  $X/N$ ) is given by equation:

$$f_{OUT} = \left( \frac{X_1}{N_1} + \frac{X_2}{N_2} + \frac{X_3}{N_3} \right) M_4 M_5 f_{REF} \quad (7)$$

Structure of synthesizer (Fig. 6) can be simply extended for more “(X/Y)” block. The  $N_1, N_2, N_3$  are fixed dividers and  $X_1, X_2, X_3$  are programmable dividers in PLL feedback. The  $M_4$  and  $M_5$  are frequency multipliers (also based on programmable dividers in feedback of PLL). These PLL are used for signal shape recover (from pulses to sine). Control block can be built with microcontroller or programmable array [10], [11].

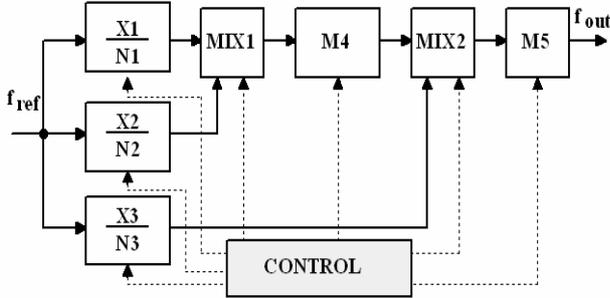


Fig. 6. Final version of frequency synthesizer with 3 blocks (X/N). The blocks  $M_4$  and  $M_5$  are PLL which acts as frequency multipliers and signal shape recover.

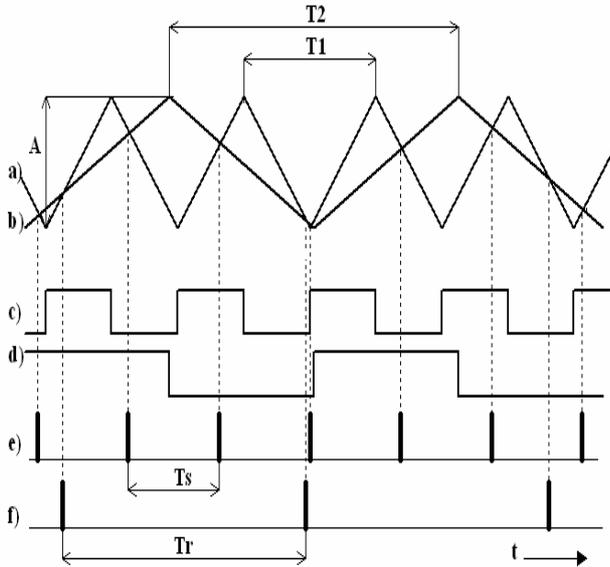


Fig. 7. Coincidence mixer time diagram. a) input signal with frequency  $f_1$  (period  $T_1$ ), b) input signal with frequency  $f_2$  (period  $T_2$ ), c) derivation of signal a), d) derivation of signal b), e) output pulses with frequency  $f_s = f_1 + f_2$  (period  $T_s$ ) f) output pulses with frequency  $f_r = \text{abs}(f_1 - f_2)$  (period  $T_r$ ).

## 2 FREQUENCY MIXER BASED ON SIGNAL COINCIDENCE

As a review, let's look at an conventional analog mixer, which performs the function of multiplication between two inputs. Analog mixing implements the following trigonometric identity:

$$C = AB = \cos(2\pi f_a t) \cos(2\pi f_b t) = \frac{1}{2} [\cos(2\pi (f_a + f_b) t) + \cos(2\pi (f_a - f_b) t)] \quad (8)$$

and bandpass filtered output  $D_s$  (depend on filter quality):

$$D_s \approx \frac{1}{2} [\cos(2\pi (f_a + f_b) t)] \quad (9)$$

for desired sum of frequencies, or lowpass (or also bandpass) output  $D_r$  for differences of frequencies:

$$D_r \approx \frac{1}{2} [\cos(2\pi |f_a - f_b| t)] \quad (10)$$

There are some problems with filtering when frequencies  $(f_a + f_b)$  and  $|f_a - f_b|$  are close each other and tuning of the output filter when frequency changing. Therefore new coincidence mixer was developed.

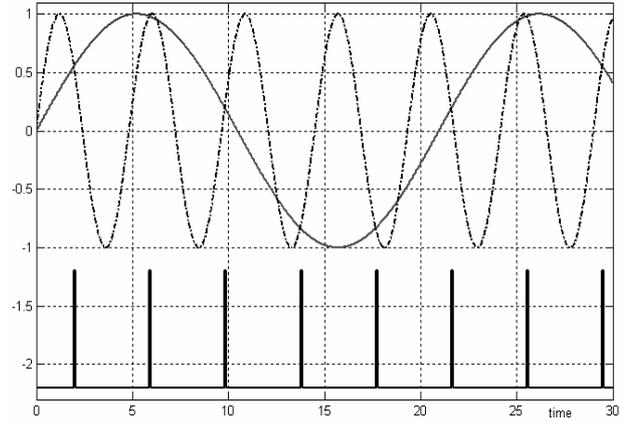


Fig. 8. Coincidence mixer - time diagram (Simulation result). Input signals (top) and output pulses (bottom). Frequency of output pulses is sum of input frequencies.

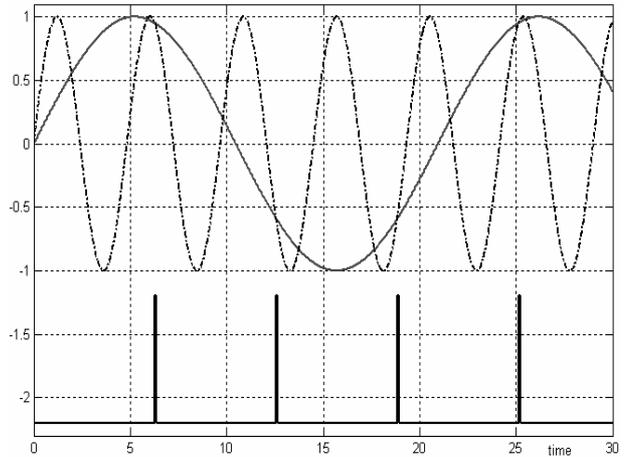


Fig. 9. Coincidence mixer - time diagram (Simulation result). Input signals (top) and output pulses (bottom). Frequency of output pulses is difference of input frequencies.

The new coincidence mixer work with input signals, which must have the same amplitude values. The principle is shown in Fig. 7, with triangle wave. The time diagrams of signals with sine wave are shown in Fig. 8. and Fig. 9.

From Fig. 8 and 9 can be seen, that coincidence mixer can generate sum and difference of input frequencies on outputs, and outputs signals shapes are pulses. In Fig. 8 and 9, the frequency of input signals were 0.3 and 1.3 [rad/sec], therefore sum output is  $0.3+1=1.6$  [rad/sec] and difference output is  $1.3-0.3=1$

[rad/sec]. The simplified block diagram of coincidence mixer is shown in Fig. 10.

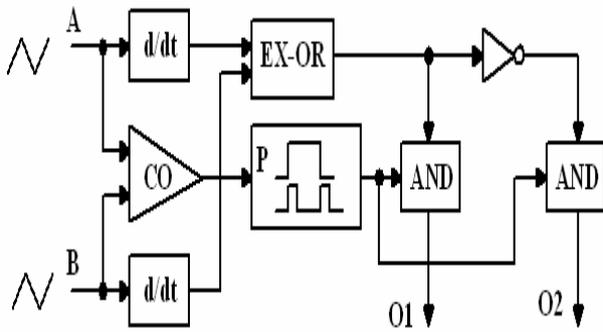


Fig. 10. Block diagram of coincidence mixer. A, B - input signals, d/dt - derivation block, CO - comparator, P - pulse block which generate pulse on rising and falling edge, EX-OR - exclusive-or gate, AND - logical and gate, O1 - output with sum of input frequencies, O2 - output with difference of input frequencies.

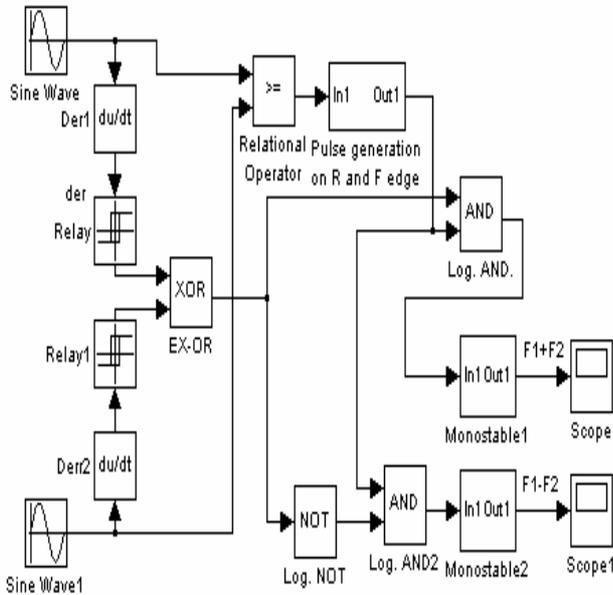


Fig. 11. Block diagram of coincidence mixer for Matlab simulation. The mixer has 2 output  $F1+F2$  and absolute value of  $F1 - F2$ . The Relay blocks are used as a converter to digital signal level.

### 3 SIMULATION RESULTS

From simulation results shown in Fig. 8 and Fig. 9 can be seen, that mixer output pulses are equally spaced and therefore good spectral purity for sum and difference frequencies.

The main drawback of this synthesizer is pulsed output and therefore PLL on output is need for recovery triangle or sine output.

The second disadvantage is: The same amplitude of input signals is need.

The first main advantage of this mixer is that no output filter is need and therefore it has a wide frequency bandwidth without any tuning.

The second advantage is almost pure digital architecture (only comparator and derivation function are not pure digital).

The third, sum and difference of frequencies can be simply generated.

Example of simulation results are shown in Fig. 12 (sine signal recovery) and Fig. 13 (frequency spectrum).

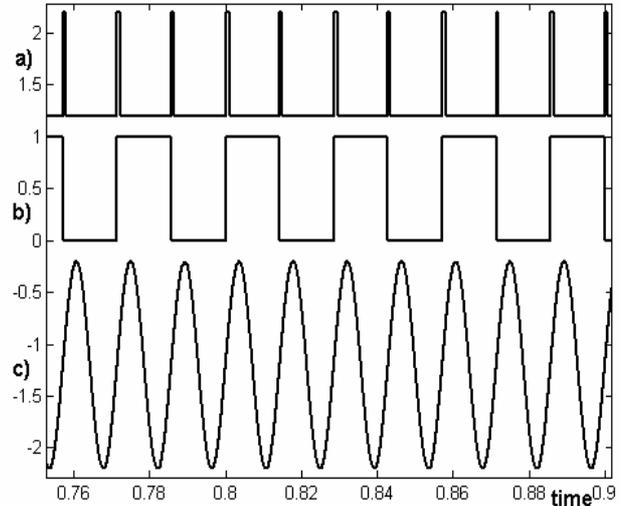


Fig. 12. The sine signal recovery. a) Mixer pulse output, b) Square wave pulses, c) Sine signal (PLL output).

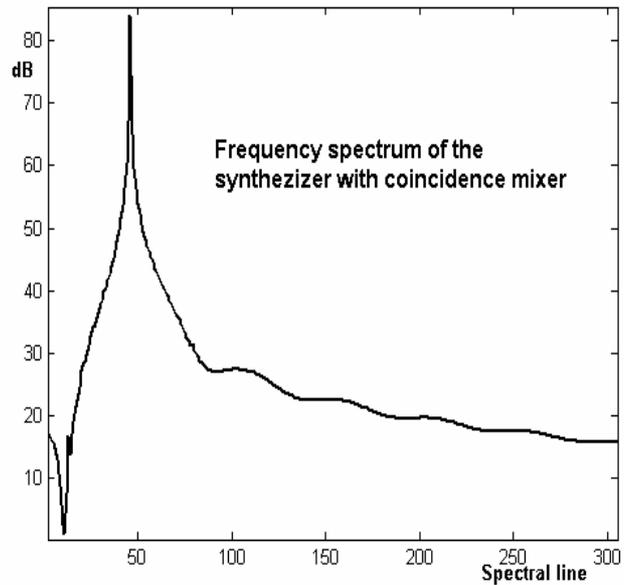


Fig. 13. Frequency spectrum of the frequency synthesizer.

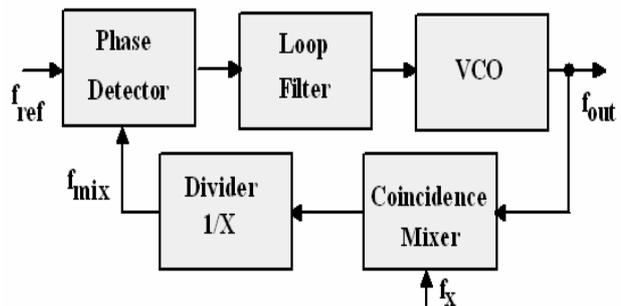


Fig. 14. The Phase-Locked-Loop with coincidence mixer and divider placed in feedback.

#### 4 FRACTIONAL FREQUENCY SYNTHESIZER WITH COINCIDENCE MIXER

The coincidence mixer can be also used directly in PLL feedback for some PLL construction. Block diagram of this system is shown in Fig. 14. For reference frequency  $f_{ref}$  and  $f_x$  frequency connected to mixer, the output frequency  $f_{out}$  is given by:

$$f_{out} = X * (f_{ref} \pm f_x) \quad (11)$$

where  $X$  is divider number in feedback of and  $\pm$  depend on mixer output (if difference or sum is used).

#### 5 CONCLUSION

A detailed look at the concept of direct frequency synthesizer with new principle of mixer, based on coincidence has been presented in this paper.

The mixer is a critical component of the frequency synthesizer. The conventional mixer converts modulated power from one frequency to another, it is sometimes called a frequency converter, but the term frequency converter usually implies a mixer/amplifier or mixer/oscillator combination. The term mixer more closely describes the mechanism through which frequency conversion occurs. Two inputs are mixed by means of nonlinearities and switching to produce a group of signals having frequencies equal to the sums and differences of the harmonics of the two input signals. The presented mixer works on another principles and have some advantages and disadvantages which was described in paper.

Analysis and simulation of the new frequency synthesizer were also shown.

#### 6 ACKOWGLEDMENT

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