Abstract – The permanent magnets used for generation of magnetic field in permanent magnet machines are placed in more or less magnetically conducting environment – electrical steel and air. This causes leakage of the magnetic flux from its desired path through the air gap. This paper describes simplified analytical calculation of magnetic properties of five most commonly used placements of permanent magnets and compares obtained leakage factors. A verification of the results via finite element method is also included.

Index Terms— Electromagnetic modelling, Finite element analysis, Magnetic flux leakage, Permanent magnets

I. NOMENCLATURE

- \( A \) magnetic vector potential
- \( b_s \) magnetic bridge width
- \( b_w \) slot opening width
- \( B_{ast} \) last defined magnetic flux density of used steel
- \( B_r \) remanent magnetic flux density
- \( B_{a} \) air gap magnetic flux density
- \( B_{a} \) leakage path magnetic flux density
- \( d \) direct axis
- \( F_{PM} \) permanent magnet magnetomotive force
- \( h_0 \) magnetic bridge height
- \( k_C \) Carter’s factor
- \( k_{g} \) air gap length factor
- \( k_{PM} \) permanent magnet leakage flux factor
- \( h_{PM} \) permanent magnet height
- \( H_c \) coercive magnetic field strength
- \( H_{ast} \) last defined magnetic field strength of steel
- \( H_a \) air gap magnetic field strength
- \( H_a \) leakage path magnetic field strength
- \( l \) iron stack length
- \( l_0 \) leakage path length
- \( q \) quadrature axis
- \( r_0 \) radius of leakage path
- \( R_{PM} \) permanent magnet reluctance
- \( R_a \) air gap reluctance
- \( R_a \) leakage path reluctance
- \( S_{o} \) area of one pole pitch in the air gap
- \( t_0 \) pole pitch
- \( t_0 \) stator slot pitch
- \( \alpha_{PM} \) mechanical permanent magnet coverage factor

\( \alpha_s \) electromagnetic pole coverage factor
\( \delta \) mechanical air gap length
\( \delta' \) electromagnetic air gap length
\( \delta_{max} \) maximal air gap above permanent magnets
\( \Delta F \) magnetomotive force drop
\( \phi_{PM} \) angle between permanent magnets
\( \Phi_{PM} \) magnetic flux of permanent magnets
\( \Phi_a \) air gap magnetic flux
\( \Phi_{PM} \) leakage magnetic flux
\( \mu_0 \) permeability of vacuum
\( \mu_{sat} \) permeability of saturated steel
\( \mu_{PM} \) permanent magnet relative permeability
\( \mu_{sat} \) relative permeability of saturated steel

II. INTRODUCTION

The precise design of permanent magnets and permanent magnet electric machines must consider possibly most effects appearing in the electric machine. This includes – among consideration of real properties of the whole magnetic circuit – also properties of the neighbourhood of the permanent magnets. It creates alternative paths to the main magnetic flux, which should go from the rotor to the stator and vice versa. These paths then lead parts of the magnetic flux, which do not assist in creation of the torque of the machine. These parts of the magnetic flux are then commonly denoted as leakage magnetic flux.

The problem of permanent magnet leakage fluxes is in the literature mentioned relatively rarely, whereas most relevant information is to be found in papers and articles. The authors often focus to one single placement of permanent magnets and study their magnetic flux leakage on order to optimize the machine design. The presented solutions are supported most often by finite element method analyses [1], [2], but analytic solutions are also presented [3], [4]. The presented papers cover traditional radial permanent magnet synchronous machines with radial or V-shaped permanent magnets [1], [2], [3], but also axial machines are often in focus of the research [4], [5] as well as transverse flux permanent magnet machines [6], [7]. As an addition to previously mentioned publication [8] adds also a calculation of leakage magnetic flux in axial area of permanent magnets.

Among traditional concepts of electric machines – or magnetic devices – the magnetic flux leakage factor is also being referred in case of non-standard rotor topologies [9] or magnetic retarders [10]. An interesting usage of leakage magnetic flux is presented in [11], where the authors use variations of leakage magnetic flux for controlling characteristics of an interior permanent magnet machine.

In above mentioned works the authors focus on problems...
of a single rotor topology, which is being analysed and evaluated without any relation to other permanent magnet placement possibilities. This article offers a unified approach for multiple topologies, which are analytically analysed and compared. For this purpose five most common permanent magnet layouts are chosen and analysed with focus to obtain a simple analytical expression of the permanent magnet leakage flux factor.

III. ANALYTICAL CALCULATION OF PERMANENT MAGNET LEAKAGE FLUX FACTOR

For comparison of their physical properties five topologies shown in Fig. 1 were chosen. They include permanent magnets placed on the surface of the rotor (layout “S”), bread-shaped permanent magnets (layout “B”), V-shaped permanent magnets layout (layout “V”), tangentially buried permanent magnets (layout “T”) and permanent magnets on the surface of the rotor equipped with pole-shoe (layout “P”). All presented designs were prepared as alternative rotor topologies for a single permanent magnet traction machine, so they were designed to have possibly closest properties, especially regarding peak air gap magnetic flux density.

A. Presumptions of the Analytic Calculations

To obtain a generally valid approach for possibly most permanent magnet rotor layouts, the following presumptions will be considered:

- The permeability of non-saturated iron is considered to be infinite, \( \mu_{Fe} \rightarrow \infty \).
- The permeability of saturated iron is considered to be given by last point of its B-H curve as \( \mu_{sat} = \frac{B_{last}}{H_{last}} \).
- The magnetic flux lines leave and enter the permanent magnet on the top and the bottom of the permanent magnet only.
- The magnetic flux density on a single leakage path is constant.

B. Analytical Model of the Magnetic Circuit

A permanent magnet placed in such an environment generates magnetomotive force, whose reaction is generation of magnetic flux. The main part of the magnetic flux goes through the air gap to the stator (main magnetic flux \( \Phi_\delta \)) and a part of the magnetic flux forms a loop on sides of the permanent magnets while another part goes through the air gap to the opposite rotor pole. Both these parts form the leakage magnetic flux \( \Phi_\sigma \).

The paths of the magnetic flux lines shown in Fig. 2 may be then substituted by a reluctance network shown in Fig. 3. Considering machine symmetry, the whole network which repeats in general \( 2p \) times may be divided by symmetry axes, i.e. \( q \)-axes of the machine.

Among the magnetomotive force of the permanent magnet \( F_{PM} \) generating the magnetic field, it includes its own (inner) magnetic reluctance \( R_{PM} \), reluctance of the air gap \( R_\delta \) and the reluctance of the leakage paths \( R_\sigma \). According to equivalent circuit shown in Fig. 3, the magnetomotive force drops equality on the air gap and leakage paths is given by magnetic field strengths and flux lines lengths as

\[
\Delta F = \oint_{\delta} H_\delta dl = \oint_{\sigma} H_\sigma dl ,
\]

whereas the magnetic flux through the air gap is known from air gap magnetic flux density and machine dimensions \[12\]

\[
\Phi_\delta = \frac{1}{S_\delta} \oint_{S_\delta} B_\delta |dS| = \alpha_\delta B_\delta t_\delta l .
\]
Since the air gap is magnetically linear environment, the air gap magnetic field strength may be derived from the air gap magnetic flux density using air permeability as

$$B_0 = \mu_0 H_0 \ .$$

(4)

C. Permanent Magnet Leakage Flux Factor

To be able to compare previously mentioned rotor topologies, it is suitable to introduce the leakage of magnetic flux as a single dimensionless factor. To be consistent with general theory of synchronous machines [12] it is possible to modify the field winding leakage factor to permanent magnet leakage flux factor defined by a ratio of permanent magnet and air gap magnetic fluxes as

$$k_a = \frac{\Phi_{PM}}{\Phi_b} \ ,$$

(5)

where the total permanent magnet magnetic flux results from the node in the equivalent circuit in Fig. 3

$$\Phi_{PM} + 2 \Phi_a + \Phi_b = 0 \ .$$

(6)

IV. PERMANENT MAGNET LEAKAGE FLUX FACTORS OF DIFFERENT ROTOR LAYOUTS

A. Permanent Magnets Placed on the Surface of the Rotor

A schematic drawing of surface mounted permanent magnet and its leakage fluxes is shown in Fig. 4. Among the main magnetic flux path through the air gap one of the leakage fluxes goes through the air gap to neighbouring magnet on opposite pole (denoted as $\sigma_1$) and a part of the magnetic flux encloses around the side of the permanent magnet (denoted as $\sigma_2$). Presuming mechanical permanent magnet pole coverage factor $\alpha_{PM}$ and machine pole pitch $t_p$, the length of the magnetic flux line between neighbouring magnets is

$$l_{\sigma_1} = (1 - \alpha_{PM}) \frac{t_p}{2} \ .$$

(7)

The length of the magnetic flux line from the top of the magnet to the rotor surface may be approximated by a quarter of a circle with radius equal to permanent magnet height $h_{PM}$, thus its length is

$$l_{\sigma_2} = \frac{1}{2} \pi h_{PM} \ ,$$

(8)

The leakage magnetic flux $\sigma_1$ uses the whole air gap length in both radial and axial directions, hence its total magnetic flux is

$$\Phi_{\sigma_1} = \int_{S_{\sigma_1}} B_{\sigma_1} dS = \int_{l} \int_{S_{\sigma_1}} B_{\sigma_1} dy dz = B_{\sigma_1} \delta l \ ,$$

(9)

whereas the magnetic flux density on this leakage path results from equality of magnetomotive force drops on the air gap and the leakage path as defined by (2), in this case

$$H_0 \delta' = H_{\sigma_1} l_{\sigma_1} \ ,$$

(10)

which gives

$$B_{\sigma_1} = \mu_0 H_{\sigma_1} = \frac{\mu_0 H_0 \delta'}{1 - \alpha_{PM} \frac{t_p}{2}} \ ,$$

(11)

where the electromagnetic air gap length $\delta'$ is its mechanical length multiplied by Carter’s factor $k_c$:

$$\delta' = k_c \delta \ .$$

(12)

In case of surface mounted permanent magnets (both “S” and “B” topologies) the air gap of the machine is increased by the thickness of permanent magnets (their material relative permeability $\mu_{PM}$ is close to the air), so the Carter’s factor is calculated from slot pitch $t_s$ and slot opening width $b_o$ as in [13]

$$k_c = \frac{t_s}{t_s - \gamma b_o} \ .$$

(13)

whereas the $\gamma$ factor includes both mechanical air gap length $\delta$ and permanent magnet thickness modified by permanent magnet permeability $\mu_{PM}$

$$\gamma = \frac{b_o}{b_o + 5 \left( \frac{h_{PM}}{\mu_{PM}} \right)} \ .$$

(14)

In case of the leakage magnetic flux $\sigma_2$, it does not leave the permanent magnet only on its top, but also on its sides. Presuming homogeneous magnetic flux density on whole cross-section of the leakage path $\sigma_3$, the total magnetic flux of this leakage path results

$$\Phi_{\sigma_2} = \int_{S_{\sigma_2}} B_{\sigma_2} dS = \int_{l} \int_{S_{\sigma_2}} B_{\sigma_2} dy dz = B_{\sigma_2} \frac{h_{PM}}{2} \ ,$$

(15)
where the magnetic flux density on this leakage path may be derived as an alternative to magnetic flux density $B_{o1}$ using

$$B_{o2} = \mu_0 H_{o2} = \frac{\delta'}{\pi \frac{r_{PM}}{2}}.$$  \hspace{1cm} (16)

For geometric layout shown in Fig. 4 the magnetic flux leakage factor results according to (5)

$$k_o = \frac{\Phi_o + 2(\Phi_{o1} + \Phi_{o2})}{\Phi_o},$$  \hspace{1cm} (17)

and after substitution and modification it gives

$$k_o = 1 + 2 \left[ \frac{2 \kappa \sigma^2}{\alpha_t (1 - \alpha_{PM} l_p)} + \frac{\kappa \sigma}{\pi \alpha_t l_p} \right].$$  \hspace{1cm} (18)

B. Bread-shaped Permanent Magnets on the Rotor Surface

By introduction of the permanent magnet curvature, its sides shorten and a wider gap is opened for the leakage magnetic flux to go between machine poles (see Fig. 5). The relation between mechanical air gap δ and air gap on the edges of the permanent magnet $\delta_{max}$ can be introduced as air gap factor

$$k_b = \frac{\delta_{max}}{\delta}. \hspace{1cm} (19)$$

Using similar approach as in section IV-A, it is necessary to modify the magnetic flux through the leakage path $\sigma_1$ to

$$\Phi_{o1} = B_{o1} k_b \delta l.$$  \hspace{1cm} (20)

The radius of the leakage path $\alpha_1$ further reduces from central permanent magnet height $h_{pm}$ to

$$r_{o2} = h_{PM} - (k_b - 1) \delta  \hspace{1cm} (21)$$

and equivalently to (15) the magnetic flux through leakage path $\sigma_2$ results

$$\Phi_{o2} = B_{o2} \frac{r_{o2}}{2} l = B_{o2} \frac{h_{PM} - (k_b - 1) \delta}{2} l.$$  \hspace{1cm} (22)

The magnetic flux density in the volume of the leakage path $\sigma_2$ is then

$$B_{o2} = \mu_0 H_{o2} = \frac{\delta'}{\pi \frac{r_{o2}}{2}} = \frac{\mu_0 H_b}{\pi \frac{r_{PM} - (k_b - 1) \delta}{2}}.$$  \hspace{1cm} (23)

The permanent magnet leakage flux factor for bread shaped permanent magnets mounted on the surface of the rotor then results

$$k_o = 1 + 2 \left[ \frac{2 \kappa \sigma^2}{\alpha_t (1 - \alpha_{PM} l_p)} + \frac{\kappa \sigma}{\pi \alpha_t l_p} \right]. \hspace{1cm} (24)$$

whereas from comparison with result (18) it is obvious, that (24) is a generalization of the relation for rectangular permanent magnets placed on the rotor surface. From the physical principle it is also evident, that identical relation will be valid for rectangular permanent magnets equipped with ferromagnetic pole-shoes, but in this case the $\gamma$ factor for calculation of Carter’s factor must be derived from mechanical air gap length only in the same way as in case of interior permanent magnets as noted below in (29).

C. Tangential Interior Permanent Magnets

In case of tangentially placed interior permanent magnets they are located in a ferromagnetic material, which significantly increases the leakage magnetic flux of the permanent magnets (see Fig. 6). To avoid excessive increase of the leakage magnetic flux, the permanent magnets are placed possibly closest to the air gap and the bridges between neighbouring poles are designed to be possibly thinnest which is further limited by mechanical constraints.

In comparison to previously analysed permanent magnet placements the main part of the leakage magnetic flux is led through (saturated) bridges between neighbouring poles (denoted as $\sigma_2$) and only a part of the leakage magnetic flux is led through parallel path in the air gap (denoted as $\sigma_1$). An additional part of the leakage magnetic flux is also present in the gap on sides of the permanent magnet, but due to hard
description of its shape it will be neglected in further calculation.

Presuming that the magnetic flux lines of both leakage paths origin in one half of the length of the bridge between the permanent magnet and the q-axis of the rotor, the length of the leakage path \( \sigma_1 \) and the radius of the leakage path \( \sigma_1 \) are identical and they are

\[
l_{\sigma_1} = r_{\sigma_1} = \frac{1}{2} \left( 1 - \alpha_{\text{PM}} \right) \frac{l_p}{2} .
\]

(25)

Presuming the leakage path \( \sigma_1 \) is a quarter of a circle, its length is

\[
l_{\sigma_1} = \pi r_{\sigma_1} = \pi \left( 1 - \alpha_{\text{PM}} \right) \frac{l_p}{8} .
\]

(26)

Similarly to previous sections, the magnetic field strength on leakage path \( \sigma_1 \) results

\[
H_{\sigma_1} = H_0 \frac{\delta'}{l_{\sigma_1}} = H_0 \frac{9 \delta'}{\pi \left( 1 - \alpha_{\text{PM}} \right) l_p} .
\]

(27)

and, presuming that the magnetic flux utilizes the whole air gap length, the magnetic flux through leakage path \( \sigma_1 \) is

\[
\Phi_{\sigma_1} = \mu_0 H_0 \frac{8 k_k k_c \delta' l}{\pi \left( 1 - \alpha_{\text{PM}} \right) l_p} .
\]

(28)

whereas in case of interior permanent magnets (topologies “V”, “T” and “P”) the curvature of magnetic flux lines in the air gap corresponds to standard electric machines, thus the \( \gamma \) factor for calculation of the Carter’s factor is obtained as

\[
\gamma = \frac{b_0}{b_0 + 5 \delta} .
\]

(29)

The magnetic field strength on leakage path \( \sigma_2 \) results from equality of magnetomotive force drops on all magnetic flux paths as

\[
H_{\sigma_2} = H_0 \frac{\delta'}{l_{\sigma_2}} ,
\]

(30)

but since this path leads through saturated steel bridge between the poles, the magnetic flux density in the bridge with height \( h_s \) results

\[
B_{\sigma_2} = \mu_{\text{sat}} H_{\sigma_2} .
\]

(31)

The magnetic flux through leakage path \( \sigma_2 \) is then

\[
\Phi_{\sigma_2} = \mu_{\text{sat}} H_0 \frac{k_c \delta h_s l}{\gamma_{\sigma_2}} .
\]

(32)

The permanent magnet leakage flux factor for tangentially placed interior permanent magnets results

\[
k_{\text{PM}} = \frac{1 + 2 \left( \frac{8 k_k k_c \delta'}{\alpha_{\text{sat}} \pi \left( 1 - \alpha_{\text{PM}} \right) l_p} + \frac{4 k_c \delta h_s}{\alpha_{\text{sat}} \left( 1 - \alpha_{\text{PM}} \right) l_p} \right)}{\mu_{\text{sat}}} ,
\]

(33)

where \( \mu_{\text{sat}} \) is the relative permeability of saturated steel derived from \( \mu_{\text{sat}} \).

D. V-shaped Interior Permanent Magnets

The V-shaped interior permanent magnets have very similar magnetic properties as the tangentially placed permanent magnets, but as an addition a central bridge in the \( d \)-axis is present (see Fig. 7). Since this bridge is located directly between permanent magnets, is is saturated in its whole length.

![Fig. 7. Leakage paths of V-shaped interior permanent magnets.](image)

Hence, to obtain the permanent magnet leakage flux factor of V-shaped interior permanent magnets it is possible to use relations derived for tangential interior permanent magnets with third leakage magnetic flux added. Since the permanent magnets are beveled from each other under angle \( \varphi_{\text{PM}} \), the length of leakage path \( \sigma_2 \) and the radius of leakage path \( \sigma_1 \) reduces to

\[
l_{\sigma_2} = r_{\sigma_1} = \frac{h_{\text{PM}}}{2} \cos \frac{\varphi_{\text{PM}}}{2} + h_s ,
\]

(34)

and in presumed geometry the length of leakage path \( \sigma_1 \) is

\[
l_{\sigma_1} = h_{\text{PM}} \sin \frac{\varphi_{\text{PM}}}{2} .
\]

(35)

The leakage magnetic flux along path \( \sigma_3 \) then results

\[
\Phi_{\sigma_3} = \mu_{\text{sat}} H_0 \frac{k_c \delta h_s l}{h_{\text{PM}} \sin \frac{\varphi_{\text{PM}}}{2}}
\]

(36)

and the leakage magnetic flux factor for V-shaped interior permanent magnets is then

1243
where

\[ k_a = 1 + 2 \cdot \frac{2 k_c k_x \delta^2}{\alpha t_p \pi \left( \frac{h_p}{2} \cos \frac{\psi_{pm} + b_y}{2} \right)} + \frac{k_c \delta h_b}{\alpha t_p} \left( \frac{h_p}{2} \cos \frac{\psi_{pm} + b_y}{2} \right) + \frac{k_c \delta b_y}{\alpha t_p} \left( \frac{h_p}{2} \cos \frac{\psi_{pm} + b_y}{2} \right). \]

(37)

V. VERIFICATION OF RESULTS USING FINITE ELEMENT METHOD

The verification of analytically obtained results was performed using open-source software FEMM [14] as a magnetostatic task. The machine used for the purpose of the study was a prototype of a 10 pole traction permanent magnet synchronous machine with 45 stator slots and rated power of 150 kW, whereas the main aim of the comparative design was keeping possibly closest total permanent magnet volume. Due to limited symmetry of the machine its whole geometry was modelled.

The material properties of used materials are shown in Tables I and II, whereas the material properties of the permanent magnets are based on minimal data sheet parameters provided by the manufacturer [15] while the parameters of the electrical steel are manufacturer’s own measured parameters from delivered samples.

<table>
<thead>
<tr>
<th>TABLE I</th>
<th>MATERIAL PROPERTIES OF USED PERMANENT MAGNETS</th>
</tr>
</thead>
<tbody>
<tr>
<td>material</td>
<td>N35UH</td>
</tr>
<tr>
<td>B [T]</td>
<td>1.17</td>
</tr>
<tr>
<td>H [A/m]</td>
<td>86000</td>
</tr>
<tr>
<td>( \mu_{sat} [H/m] )</td>
<td>1.08</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>TABLE II</th>
<th>MATERIAL PROPERTIES OF USED LAMINATION (SELECTION OF MOST SIGNIFICANT POINTS)</th>
</tr>
</thead>
<tbody>
<tr>
<td>material</td>
<td>M330-50A</td>
</tr>
<tr>
<td>B [T]</td>
<td>1.5</td>
</tr>
<tr>
<td>H [A/m]</td>
<td>5590</td>
</tr>
</tbody>
</table>

The permanent magnet leakage flux factor was derived from magnetic flux going from the rotor to the stator over one pole pitch as

\[ \Phi_s = \oint \frac{B_n}{\delta} dS, \]

(38)

where the values of air gap magnetic flux density \( B_n \) were read on a line drawn on inner surface of the stator. The total magnetic flux generated by permanent magnets was then derived from maxima and minima of the magnetic vector potential in the whole task [16] as

\[ \Phi_{pm} = (A_{\max} - A_{\min}) \delta, \]

(39)

where \( \delta \) is the task depth (\( \delta = 0.286 \) m).

The permanent magnet leakage flux factor is then calculated using (5). The summary of obtained results is listed in Table III, the magnetic flux lines obtained from the simulations are shown in Fig. 8.

<table>
<thead>
<tr>
<th>TABLE III</th>
<th>RESULTS OBTAINED USING FINITE ELEMENT METHOD</th>
</tr>
</thead>
<tbody>
<tr>
<td>magnet layout</td>
<td>S</td>
</tr>
<tr>
<td>( \Phi_s [mWb] )</td>
<td>18.18</td>
</tr>
<tr>
<td>( A_{\max} [B/m] )</td>
<td>0.032486</td>
</tr>
<tr>
<td>( A_{\min} [B/m] )</td>
<td>-0.032505</td>
</tr>
<tr>
<td>( \Phi_{pm} [mWb] )</td>
<td>18.59</td>
</tr>
<tr>
<td>( k ) [%]</td>
<td>1.022</td>
</tr>
</tbody>
</table>

The analytically calculated results according to relations (18), (24), (33) and (37) and their comparison with results from the finite element method analysis are shown in Table IV. The percentual difference between the results was calculated as

\[ \delta k_a = \frac{k_a - k_{a,FEM}}{k_{a,FEM}} \cdot 100 \% . \]

(40)

Fig. 8. Details of magnetic flux lines of leakage magnetic fluxes in layouts “S”, “B”, “P”, “T” and “V” (left-to-right).
TABLE IV
COMPARISON OF RESULTS OF ANALYTICAL CALCULATION WITH FEM

<table>
<thead>
<tr>
<th>layout</th>
<th>$k_s$ [-]</th>
<th>$k_{asm}$ [-]</th>
<th>$\delta k_s$ [%]</th>
</tr>
</thead>
<tbody>
<tr>
<td>S</td>
<td>1.028</td>
<td>1.022</td>
<td>0.59</td>
</tr>
<tr>
<td>B</td>
<td>1.037</td>
<td>1.026</td>
<td>1.04</td>
</tr>
<tr>
<td>V</td>
<td>1.264</td>
<td>1.275</td>
<td>-0.92</td>
</tr>
<tr>
<td>T</td>
<td>1.210</td>
<td>1.266</td>
<td>-4.39</td>
</tr>
<tr>
<td>P</td>
<td>1.031</td>
<td>1.026</td>
<td>0.57</td>
</tr>
</tbody>
</table>

VI. CONCLUSION

Although the presented analytical approach to calculation of permanent magnet leakage fluxes uses many simplifying conditions, the results of analytical calculations correspond with finite element method analyses in order of per cent. When comparing the obtained results with results derived in other literature they correspond also with results obtained using different approaches. This means that derived relations may be successfully used for design of permanent magnets in most common rotor topologies, while the simplicity of obtained solution allows fast calculation of the permanent magnet leakage factor and implementation of such a calculation into a higher algorithm.

The comparison of results between different rotor layouts show, that lowest leakage magnetic flux appears when permanent magnets are not placed in ferromagnetic environment, which corresponds to surface mounted permanent magnets. The placement of permanent magnets into ferromagnetic environment (interior permanent magnets) increases the permanent magnet leakage flux, so it may reach up to 25 per cent of the air gap magnetic flux.

As a result the interior permanent magnet layouts are least advantageous from material consumption point of view since they require approximately 25 per cent higher mass of permanent magnets to achieve identical air gap magnetic flux as the surface mounted permanent magnets. As a counter point another advantages of interior permanent magnets have to be considered - lower effect of air gap harmonic components regarding permanent magnet losses and higher saliency resulting in additional reluctance torque of interior permanent magnet machine.

VII. REFERENCES


VIII. BIOGRAPHIES

K. Hruska (M’20) was born in Ostrov in the Czechoslovak Socialist Republic on January 16, 1983. He graduated from the University of West Bohemia in 2007.

Since 2018 he is a reader at the Faculty of Electrical Engineering, University of West Bohemia. He lectures courses of electric machines, theory of electric machines and design of electric machines. As a member of Research and Innovation Centre for Electrical Engineering he leads the Electric Machine Group and he is active in research and development related to electric machines.

P. Dvorak (M’16) was born in Litomerice in the Czechoslovak Socialist Republic on April 29, 1978. He graduated from the University of West Bohemia in 2003.

Since 2005 he is employed in SKODA ELECTRIC a.s. Since 2014 he works as a researcher in Research and Development Department of the SKODA ELECTRIC and his activity is focused on research of the traction drives based on asynchronous motors and synchronous motors with permanent magnets for wheel propulsion of public transport vehicles.